

제 6 장 직류변환장치

DC to DC Converter DC → DC

6.1 개요

- AC의 전력변환: 변압기를 사용 쉽게 가능함
- DC의 전력변환: 변압기로는 어려움
- DC-DC Converter를 사용하면 가능
- 종류
 - 강압 초퍼(Buck chopper)
 - 승압 초퍼(Boost chopper)
 - 강압 및 승압 초퍼(Buck & Boost chopper)

6.2 Basic Switching Converter



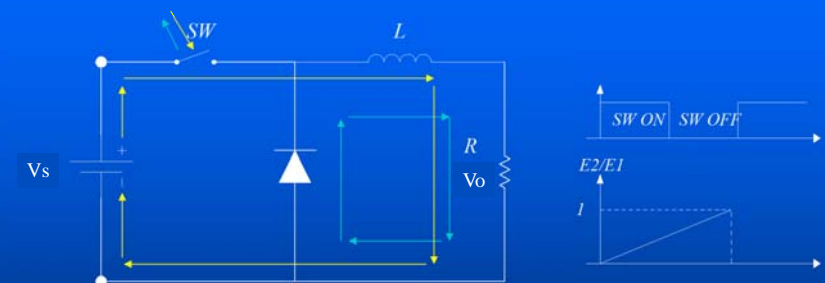
- Switching 방식에 의한 DC 제어

$$V_o = \frac{1}{T} \int_0^T v_o(t) dt = \frac{1}{T} \int_0^{DT} V_s(t) dt$$

$$= \frac{V_s}{T} \int_0^{DT} 1 dt = \frac{V_s}{T} [t]_0^{DT} = \frac{V_s}{T} (DT - 0) = V_s D$$

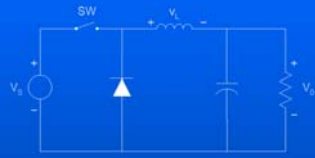
- Duty Cycle(D)=Switch On 시간(DT)/주기(T)

6.3 강압: Buck Converter(Step-down)



- 입력(V_s) 보다 출력(V_o) 이 작음

6.3 Buck Converter: 전압



■ Switch On

$$v_L = V_s - V_o = L \frac{di_L}{dt} = L \frac{\Delta i_L}{\Delta t} = L \frac{\Delta i_L}{DT}$$

$$\therefore \Delta i_L = \frac{1}{L} (V_s - V_o) DT$$

■ Switch Off

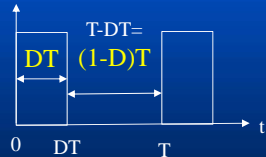
$$v_L = -V_o = L \frac{di_L}{dt} = L \frac{\Delta i_L}{\Delta t} = L \frac{\Delta i_L}{(1-D)T}$$

$$\therefore \Delta i_L = -\frac{1}{L} V_o (1-D)T$$

■ 충전전류+방전전류=0

$$\frac{1}{L} (V_s - V_o) DT - \frac{1}{L} V_o (1-D)T = 0$$

$$V_s D - V_o D - V_o + V_o D = 0 \quad \therefore V_o = V_s D$$

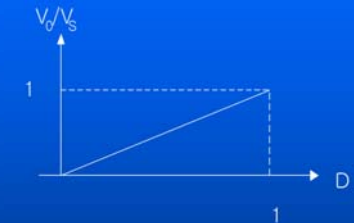


6.3 Buck Converter: 출력

■ 충전전류+방전전류=0

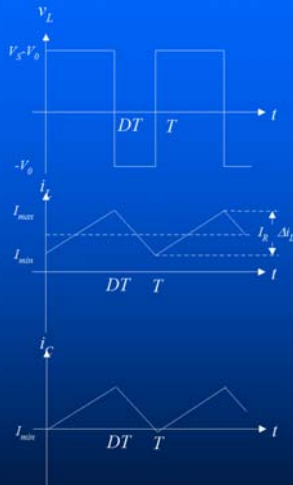
$$D \leq 1, \quad V_o = V_s D, \quad \therefore \frac{V_o}{V_s} = D$$

D	출력/입력 (V_o/V_s)
0	0
0.2	0.2
0.5	0.5
0.8	0.8
1.0	1.0



- 강압(Step-down)
- 입력 대비 출력이 낮음

6.3 Buck Converter: 리플



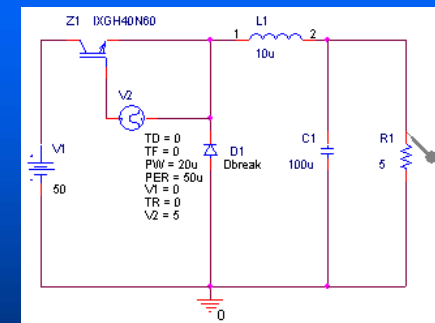
■ Ripple

$$v_L = -V_o = L \frac{di_L}{dt}$$

$$\frac{\Delta i_L}{\Delta t} = \frac{\Delta i_L}{(1-D)T} = -\frac{1}{L} V_o$$

$$\Delta i_L = (1-D)T \left(-\frac{1}{L} V_o \right)$$

예제 6-1 벅 변환기



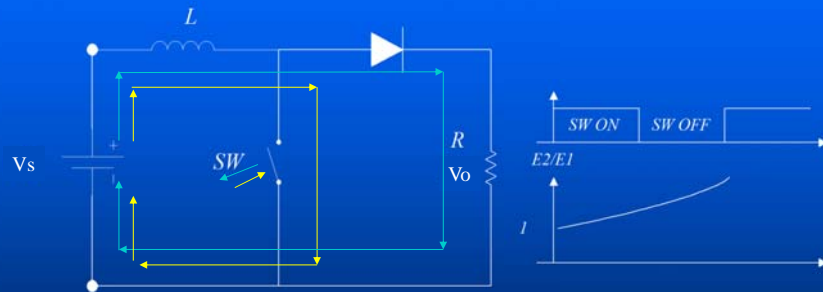
■ Parameter

- ✓ $V_s = 50 \text{ V}$
- ✓ $L = 10 \mu\text{H}$
- ✓ $C = 100 \mu\text{F}$
- ✓ $f = 20 \text{ kHz} (T = 50 \mu\text{s})$
- ✓ $D = 0.4 (T = 20 \mu\text{s})$
- ✓ $R = 20 \text{ ohm}$
- ✓ Step
- ✓ = 0 1 ms

■ Find

- ✓ 출력전압
- ✓ 전류 최대, 최소값

6.5 승압: Boost Converter(Step-up)



■ 입력(V_s) 보다 출력(V_o) 이 커짐

6.3 Boost Converter: 전압



■ Switch On

$$v_L = V_s = L \frac{di_L}{dt} = L \frac{\Delta i_L}{\Delta t} = L \frac{\Delta i_L}{DT}$$

$$\therefore \Delta i_L = \frac{1}{L} V_s DT$$

■ Switch Off

$$v_L = V_s - V_o = L \frac{di_L}{dt} = L \frac{\Delta i_L}{\Delta t} = L \frac{\Delta i_L}{(1-D)T}$$

$$\therefore \Delta i_L = \frac{1}{L} (V_s - V_o)(1-D)T$$

■ 충전전류+방전전류=0

$$\frac{1}{L} V_s DT + \frac{1}{L} (V_s - V_o)(1-D)T = 0$$

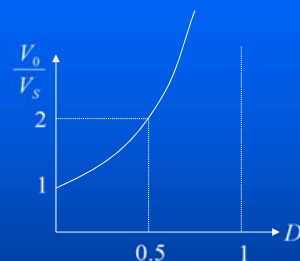
$$\cancel{V_s D} + \cancel{V_s} D - \cancel{V_o} D + V_o D = 0 \quad \therefore V_o = \frac{V_s}{(1-D)}$$

6.5 Boost Converter: 출력

■ 충전전류+방전전류=0

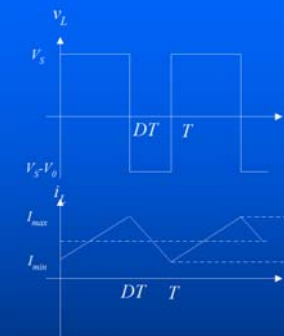
$$D \leq 1, V_o = \frac{V_s}{(1-D)}, \therefore \frac{V_o}{V_s} = \frac{1}{(1-D)}$$

D	출력/입력	(V_o/V_s)
0	$1/(1-0)$	1
0.2	$1/(1-0.2)$	1.25
0.5	$1/(1-0.5)$	2.0
0.8	$1/(1-0.8)$	5.0
1.0	$1/(1-1)$	∞



■ 승압(Step-up)
■ 입력 대비 출력이 높음

6.5 Boost Converter: 인덕터전류



■ 인덕터의 평균전류

$$V_s I_L = \frac{V_o^2}{R} = \frac{\left(\frac{V_o}{(1-D)}\right)^2}{R} = \frac{V_s^2}{(1-D)^2 R}$$

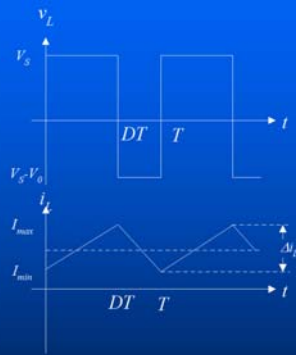
$$\therefore I_L = \frac{V_s}{(1-D)^2 R}$$

■ 인덕터의 전류 최소, 최대값

$$\left(\because \frac{\Delta i_L}{\Delta t} = \frac{\Delta i_L}{DT} = \frac{V_s}{L} \right) \rightarrow I_{\max} = I_L + \frac{\Delta i_L}{2} = \frac{V_s}{(1-D)^2 R} + \frac{V_s DT}{2L}$$

$$I_{\min} = I_L - \frac{\Delta i_L}{2} = \frac{V_s}{(1-D)^2 R} - \frac{V_s DT}{2L}$$

6.5 Boost Converter: 스위칭 주파수



- 전류의 연속조건: 최소 값이 0 보다 커야함

$$I_{\min} = 0 = \frac{V_s}{(1-D)^2 R} - \frac{V_s DT}{2L}$$

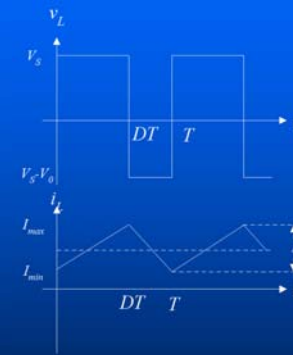
$$\frac{V_s}{(1-D)^2 R} = \frac{V_s DT}{2L} = \frac{V_s D}{2Lf}$$

- 인덕터 및 스위치의 조합

$$(Lf)_{\min} = \frac{D(1-D)^2 R}{2}$$

$$\therefore L_{\min} = \frac{D(1-D)^2 R}{2f}$$

6.5 Boost Converter: 전압의 맥동



- 커패시터 전하 변화량

$$|\Delta Q| = \left(\frac{V_o}{R} \right) DT = C \Delta V_o$$

- 맥동

$$\Delta V_o = \frac{V_o DT}{RC} = \frac{V_o D}{RCf}$$

$$\frac{\Delta V_o}{V_o} = \frac{DT}{RC} = \frac{D}{RCf}$$

예제 6-3 부스트 변환기의 설계

- 12V→30V로 승압, 맥동율: 1% 미만, R=50ohm

- Duty 비

$$\frac{V_o}{V_s} = \frac{1}{(1-D)}, \quad D = 1 - \frac{V_o}{V_s} = 1 - \frac{12}{30}$$

- 인덕터 최소값: f=25kHz로 함(가정주파수 보다 높게)

$$L_{\min} = \frac{D(1-D)^2 R}{2f} = \frac{0.6(1-0.6)^2 50}{2(25000)} = 96 \mu H$$

예제 6-3 부스트 변환기의 설계(2)

- 인덕터 전류

$$I_L = \frac{V_s}{(1-D)^2 R} = \frac{12}{(1-0.6)^2 50} = 1.5 A$$

$$\frac{\Delta i_L}{2} = \frac{V_s D}{2Lf} = \frac{(12)(0.6)}{2(120 \times 10^{-6})(25000)} = 1.2 A$$

$$I_{\max} = 1.5 + 1.2 = 2.7 A$$

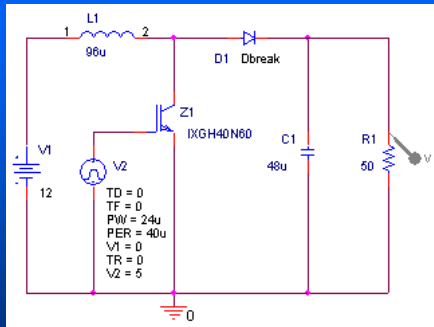
$$I_{\min} = 1.5 - 1.2 = 0.3 A$$

- 인덕터 전류

$$\frac{\Delta V_o}{V_o} < 1\%$$

$$C \geq \frac{D}{Rf(\Delta V_o/V_o)} = \frac{0.6}{(50)(25 \times 10^3)(0.01)} = 48 \mu F$$

예제 6-3 부스트 변환기(Pspice 해)



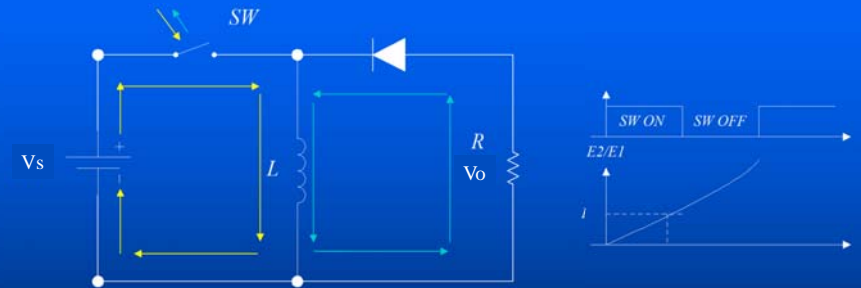
■ Parameter

- ✓ $V_S = 12\text{ V}$
- ✓ $L = 96\text{ }\mu\text{H}$
- ✓ $C = 48\text{ }\mu\text{F}$
- ✓ $f = 25\text{ kHz}$ ($T = 40\text{ }\mu\text{s}$)
- ✓ $D = 0.6$ ($D = 24\text{ }\mu\text{s}$)
- ✓ $R = 50\text{ ohm}$
- ✓ Step
= 0 1 ms

■ Find

- ✓ 출력전압
- ✓ 전류 최대, 최소값

6.6 강압 및 승압: Buck-Boost Converter



■ 입력(V_S) 보다 출력(V_O) 이 $D=0.5$ 이상이면 커짐

6.3 Buck-Boost Converter: 전압



■ Switch On

$$v_L = V_S = L \frac{di_L}{dt} = L \frac{\Delta i_L}{\Delta t} = L \frac{\Delta i_L}{DT}$$

$$\therefore \Delta i_L = \frac{1}{L} V_S DT$$

■ Switch Off

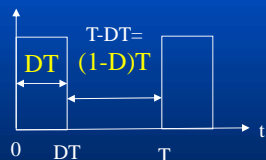
$$v_L = -V_O = L \frac{di_L}{dt} = L \frac{\Delta i_L}{\Delta t} = L \frac{\Delta i_L}{(1-D)T}$$

$$\therefore \Delta i_L = -\frac{1}{L} V_O (1-D)T$$

■ 충전전류+방전전류=0

$$\frac{1}{L} V_S DT - \frac{1}{L} V_O (1-D)T = 0$$

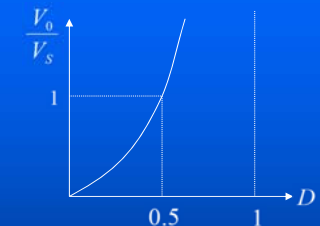
$$V_S D - V_O + V_O D = 0 \quad \therefore V_O = \frac{V_S D}{(1-D)}$$



6.6 Buck-Boost Converter: 출력

■ 충전전류+방전전류=0

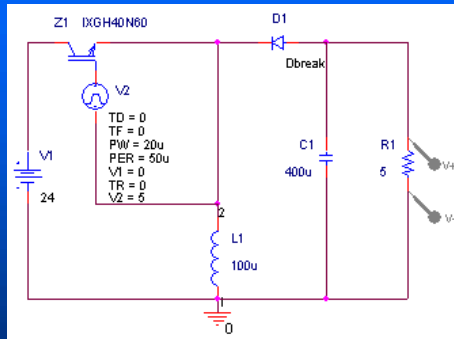
$$D \leq 1, \quad V_O = V_S \frac{D}{(1-D)}, \quad \therefore \frac{V_O}{V_S} = \frac{D}{(1-D)}$$



D	출력/입력	(V_O/V_S)
0	$0/(1-0)$	0
0.2	$0.2/(1-0.2)$	0.25
0.5	$0.5/(1-0.5)$	1.0
0.8	$0.8/(1-0.8)$	4.0
1.0	$1/(1-1)$	∞

- 강압 및 승압 (Step-up & down)
- 입력 대비 출력이 낮거나 높음

예제 6-4 벡-부스트 변환기(Pspice 해)



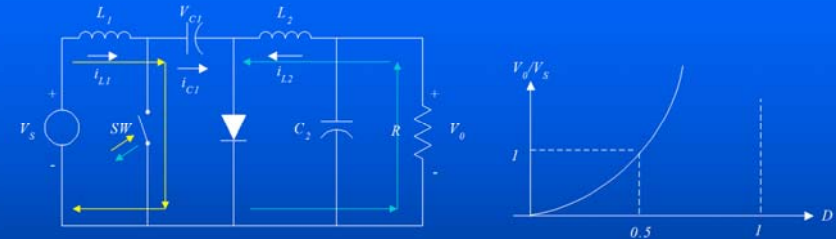
■ Parameter

- ✓ $V_S = 24\text{ V}$
- ✓ $R = 5\text{ ohm}$
- ✓ $L = 100\text{ }\mu\text{H}$
- ✓ $C = 400\text{ }\mu\text{F}$
- ✓ $f = 25\text{ kHz}$ ($T = 40\text{ }\mu\text{s}$)
- ✓ $D = 0.6$ ($D = 24\text{ }\mu\text{s}$)
- ✓ Step
= 0 0.5 ms

■ Find

- ✓ 출력전압
- ✓ 전류 최대, 최소값

6.6 Cuk Converter



- 입력(E_1) VS 출력(E_2) 이 적거나 커짐

6.7 Cuk Converter: 전압



■ Switch On

$$V_{C1} = V_S - V_0$$

$$(i_{C1})_{closed} = -I_{L2}$$

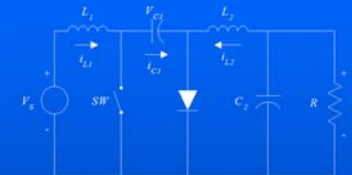
■ Switch Off

$$(i_{C1})_{open} = I_{L1}$$

■ 충전전류+방전전류=0

$$-i_{L2}DT + i_{L1}(1-D)T = 0, \quad \frac{i_{L1}}{i_{L2}} = \frac{D}{(1-D)}$$

6.7 Cuk Converter: 출력



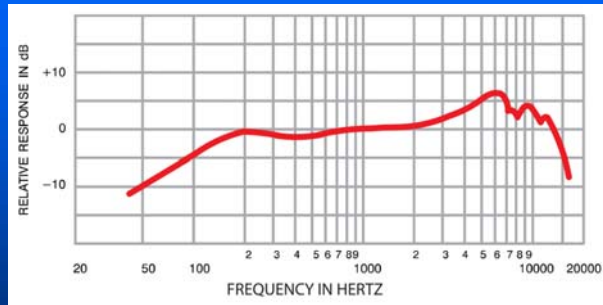
■ 공급전력=소모전력

$$P_S = P_0$$

$$V_S i_{L1} = -V_0 i_{L2}, \quad \frac{i_{L1}}{i_{L2}} = \frac{-V_0}{V_S}$$

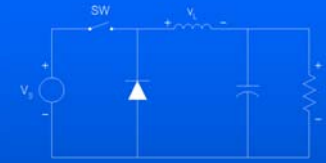
$$\therefore \frac{V_0}{V_S} = -\frac{D}{(1-D)}, \quad \left(\because \frac{i_{L1}}{i_{L2}} = \frac{D}{(1-D)} \right)$$

Switching Frequency



- Audio frequency(가청주파수)을 벗어나는 20kHz 이상의 초음파(ultra sonic) 영역에서 스위칭

DC-DC Converter 종합



- Buck: 강압



- Boost : 승압



- Buck-boost: 승압/강압



- Cuk: 승압/강압